

# Neuronale Netze

# Funktionen

**Definition:** Gegeben seien die Mengen

$D$  (Definitionsbereich) und  $W$  (Wertebereich).

Eine Funktion  $f : D \rightarrow W$  ordnet jedem  $x \in D$  genau ein  $y = f(x) \in W$  zu:

$$D \ni x \quad \longrightarrow \quad y = f(x) \in W.$$

**Satz:** Eine Funktion  $f : D \rightarrow W$  ist äquivalent charakterisiert durch

- a) die Auswertungsvorschrift von  $f$  oder
- b) den Graph  $G = \{(x, f(x)) \in D \times W \mid x \in D\}$  von  $f$ .

## Einfache und „komplizierte“ Funktionen

$$\mathbb{R} \ni x \longrightarrow y = x^2 \quad \in \mathbb{R}$$

$$\mathbb{R} \ni x \longrightarrow y = e^{-x^2} \quad \in \mathbb{R}$$

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$$\text{Restaurant-Gäste} \ni x \longrightarrow y = \text{will } x \text{ bestellen} \in \text{Speisekarte}$$

$$\text{Urlaubs-Fotos} \ni x \longrightarrow y = x \text{ zeigt ein Pferd} \in \{\text{ja, nein}\}$$

$$\text{Proteomics-Daten} \ni x \longrightarrow y = x \text{ hat Krebs} \in \{\text{ja, nein}\}$$

$$\text{Instagram-Daten} \ni x \longrightarrow y = x \text{ ist depressiv} \in \{\text{ja, nein}\}$$

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**Darstellung:**  $\mathbb{R}^n \ni x \rightarrow y = f(x) \in \mathbb{R}^m$  (Zahlen statt Objekte)

a) Auswertungsvorschrift?      b) Graph  $G = \{(x, f(x)) \mid x \in D\}$ ?

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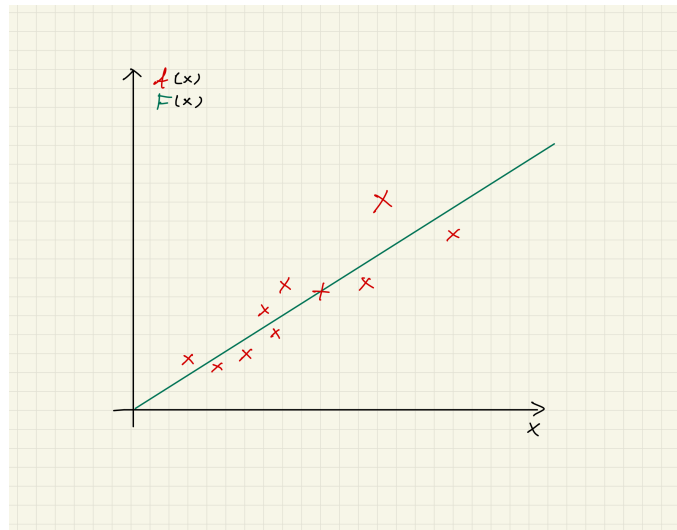
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**Ausweg:** Approximation basierend auf Daten:

Wertetabelle:  $G_N = \{(x, f(x)) \in D \times W \mid x \in D_N \subset D\}$

# Ausgleichsproblem

Daten:  $(x_i, y_i)$ ,  $y_i = f(x_i)$ .  $i = 1, \dots, N$



parametrisierte Ansatzfunktion:  $F_w(x) = wx$ ,  $w \in \mathbb{R}$

Bestimme den Parameter  $w$  so, dass  $F_w$  die Funktion  $f$  „gut“ approximiert!

# Ausgleichsproblem

Fehlerfunktional:

$$\mathcal{J}(w) = \sum_{i=1}^N (F_w(x_i) - y_i)^2 = \sum_{i=1}^N (wx_i - y_i)^2$$

Minimierungsproblem:

$$w \in \mathbb{R} : \quad \mathcal{J}(w) \leq \mathcal{J}(v) \quad \forall v \in \mathbb{R}$$

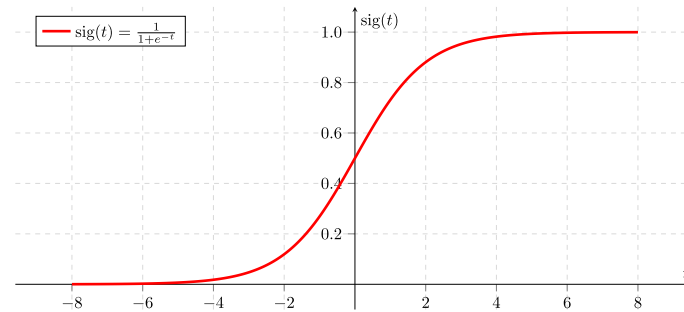
Lösung:

$$\mathcal{J}'(w) = 2 \sum_{i=1}^N (wx_i - y_i)x_i \stackrel{!}{=} 0 \quad w = \left( \sum_{i=1}^N y_i x_i \right) / \left( \sum_{i=1}^N x_i^2 \right)$$



## Neuronales Netz (1 Neuron)

Aktivierungsfunktion:  $\sigma = 1/(1 + \kappa e^{-x})$



1 Schicht:  $F_{w,b}(x) = \sigma(wx + b)$ , Parameter  $w, b \in \mathbb{R}$

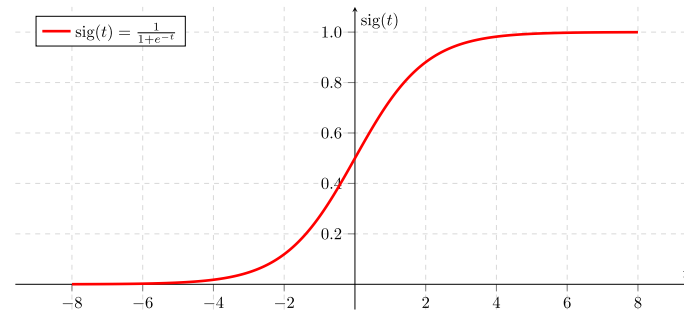
2 Schichten:

$$F_{W,b}(x) = \sigma(w_2\sigma(w_1x + b_1) + b_2) = g_2 \circ g_1(x), \quad g_i(z) = \sigma(w_i z + b_i)$$

Parameter  $w_1, w_2, b_1, b_2 \in \mathbb{R}$

# Tiefes Neuronales Netz (Deep Neural Network, 1 Neuron)

Aktivierungsfunktion:  $\sigma(x) = 1/(1 + \kappa e^{-x})$



L Schichten:

$$F_{W,b}(x) = g_L \circ g_{L-1} \circ \cdots \circ g_1(x), \quad g_i(z) = \sigma(w_i z + b_i)$$

Parameter  $w_i, b_i \in \mathbb{R}, \quad i = 1, \dots, L$

# Neuronales Netz

L Schichten (Deep Neural Network):

$$F_{W,b}(x) = g_L \circ g_{L-1} \circ \dots \circ g_1(x), \quad g_i(z) = \sigma(W_i z + b_i), \quad W_i \in \mathbb{R}^{n_i, n_{i-1}}, \quad b_i \in \mathbb{R}^{n_i}$$

von  $n_{i-1}$  nach  $n_i$  Neuronen:

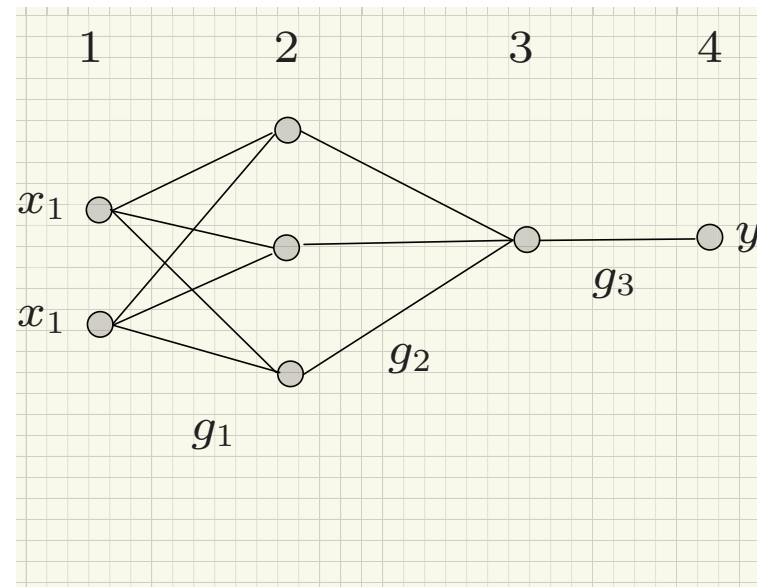
$$\mathbb{R}^{n_{i-1}} \ni z \mapsto g_i(z) = \sigma(W_i z + b_i) = \begin{pmatrix} \sigma((W_i z)_1 + b_{i,1}) \\ \vdots \\ \sigma((W_i z)_{n_i} + b_{i,n_i}) \end{pmatrix} \in \mathbb{R}^{n_i}$$

Parameter:  $W = (W_1, \dots, W_L), \quad b = (b_1, \dots, b_L)$

# Neuronales Netz: Schematische Darstellung

4 Schichten (Deep Neural Network):

$$F_{W,b}(x) = g_3 \circ g_2 \circ g_1(x), \quad g_i(z) = \sigma(W_i z + b_i), \quad i = 1, 2, 3$$



## Neuronales Netz: Parameter

4 Schichten (Deep Neural Network):

$$F_{W,b}(x) = g_3 \circ g_2 \circ g_1(x), \quad g_i(z) = \sigma(W_i z + b_i), \quad i = 1, 2, 3$$

Parameter:  $W = (W_1, W_2, W_3)$ ,  $b = (b_1, b_2, b_3)$

$$W_1 = \begin{pmatrix} W_{1,11} & W_{1,12} \\ W_{1,21} & W_{1,22} \\ W_{1,31} & W_{1,32} \end{pmatrix} \in \mathbb{R}^{3,2}, \quad b_1 = \begin{pmatrix} b_{1,1} \\ b_{1,2} \\ b_{1,3} \end{pmatrix} \in \mathbb{R}^3,$$

$$W_2 = (W_{2,11} \quad W_{2,12} \quad W_{2,13}) \in \mathbb{R}^{1,3}, \quad b_2 = (b_{2,1}) \in \mathbb{R}$$

$$W_3 = (W_{3,11}) \in \mathbb{R}, \quad b_3 = (b_{3,1}) \in \mathbb{R}$$

## Bestimmung der Parameter: Ausgleichsproblem

Daten:  $(x_i, y_i)$ ,  $y_i = f(x_i)$ ,  $i = 1, \dots, N$

Fehlerfunktional:

$$\mathbb{R}^{n_1(n_0+1)+\dots+n_L(n_{L-1}+1)} \ni \mathcal{J}(W, b) = \sum_{i=1}^N (F_{W,b}(x_i) - y_i)^2 \rightarrow \mathbb{R}$$

Methode des steilsten Abstiegs: **Achtung: Lokale Minima!!**



# Anwendung: Diagnose von Krankheiten

**Funktion:**  $\{\text{Proteom}\} \ni x \mapsto f(x) = y \in \{\text{Klassen}\}$

## Deep Learning for Proteomics Data for Feature Selection and Classification

Sahar Iravani<sup>1</sup>[0000-0002-8923-326X] and Tim O.F.  
Conrad<sup>2,3</sup>[0000-0002-5590-5726]

<sup>1</sup> Zuse institute Berlin, Takustrasse 7, 14195 Berlin, Germany  
[iravani@zib.de](mailto:iravani@zib.de)

<sup>2</sup> Zuse institute Berlin, Takustrasse 7, 14195 Berlin, Germany

<sup>3</sup> Free University of Berlin, Arnimallee 6, 14195 Berlin, Germany  
[conrad@math.fu-berlin.de](mailto:conrad@math.fu-berlin.de)

Iravani S., Conrad T.O.F. (2019) Deep Learning for Proteomics Data for Feature Selection and Classification. In: Holzinger A., Kieseberg P., Tjoa A., Weippl E. (eds) Machine Learning and Knowledge Extraction. CD-MAKE 2019. Lecture Notes in Computer Science, vol 11713. Springer, Cham.

# Anwendung: Diagnose von Depressionen

**Funktion:**  $\{\text{Instagram-Daten}\} \ni x \mapsto f(x) = y \in \{\text{depressiv, nicht depressiv}\}$

**Daten:** bekannte Diagnosen  $f(x_i) = y_i, i = 1, \dots, N$

## This AI System Can Diagnose Depression From Instagram Photos

Researchers created a machine-learning algorithm that was able to identify clinical depression with 70 percent accuracy, while human general practitioners achieved a 42 percent success rate.

By Glenn McDonald Published on 8/9/2017 at 2:25 PM

Heads up Instagram users — the pictures you post may be more revealing than you think.

This week, researchers at Harvard University and the University of Vermont released a study that suggests artificial intelligence systems can identify a depressed individual simply by looking at their Instagram photos.

According to the researchers, their algorithm has a 70 percent success rate when determining which Instagram users have been diagnosed as clinically depressed within the last three years. By comparison, general practitioners have about a 42 percent success rate when diagnosing depression through in-person evaluations. While those figures aren't particularly rigorous from a statistical point of view — more on that in a bit — they do suggest that AI could be useful in screening for clinical depression.

See <er (2017)

Regular article | [Open Access](#) | Published: 08 August 2017

### Instagram photos reveal predictive markers of depression

[Andrew G Reece](#) & [Christopher M Danforth](#)

*EPJ Data Science* 6, Article number: 15 (2017) | [Cite this article](#)

204k Accesses | 83 Citations | 3411 Altmetric | [Metrics](#)

**i** This article has been updated

**i** The [Erratum](#) to this article has been published in *EPJ Data Science* 2017 6:21

#### Abstract

Using Instagram data from 166 individuals, we applied machine learning tools to successfully identify markers of depression. Statistical features were computationally extracted from 43,950 participant Instagram photos, using color analysis, metadata components, and algorithmic face detection. Resulting models outperformed general practitioners' average unassisted diagnostic success rate for depression. These results held even when the analysis was restricted to posts made before depressed individuals were first diagnosed. Human ratings of photo attributes (happy, sad, etc.) were weaker predictors of depression, and were uncorrelated with computationally-generated features. These results suggest new avenues for early screening and detection of mental illness.

A.G. Reece., C.M. Danforth: Instagram photos reveal predictive markers of depression. *EPJ Data Sci.* 6, 15 (2017).



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## Anwendung: Urlaubs-Fotos

Klassifizierung von Urlaubs-Fotos: Bild zeigt einen: Panda, Stoppschild,...

Funktion:  $\{\text{Pixel-Matrizen}\} \ni x \mapsto f(x) = y \in \{\text{Klassen}\}$

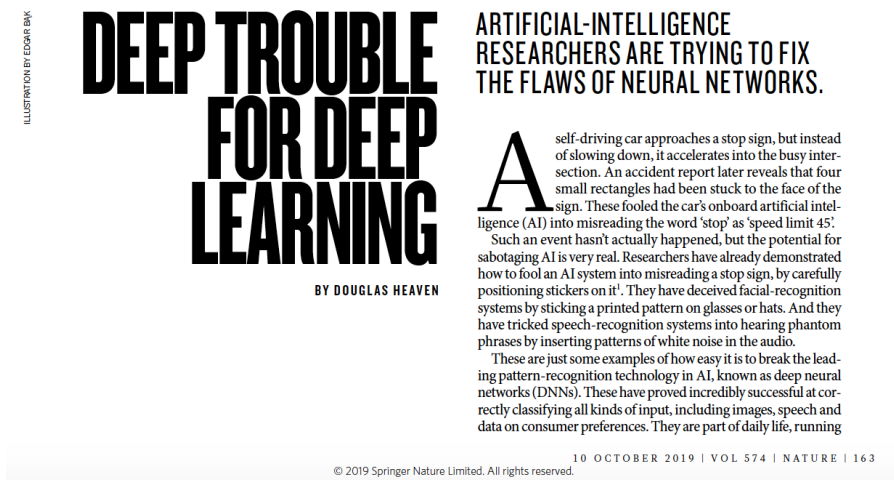
Daten: klassifizierte Urlaubs-Fotos  $f(x_i) = y_i, i = 1, \dots, N$

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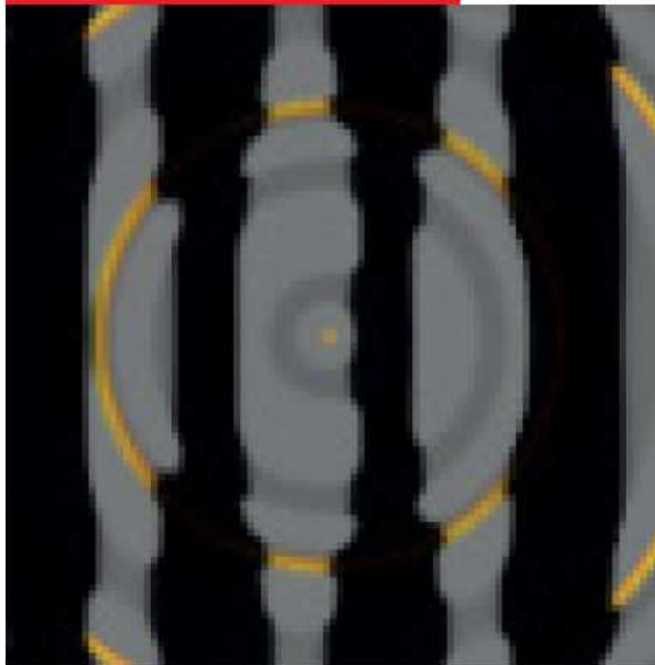
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D. Heaven: Deep Trouble for Deep learning. Nature 163 (2019)

# Tiefe Fantasie

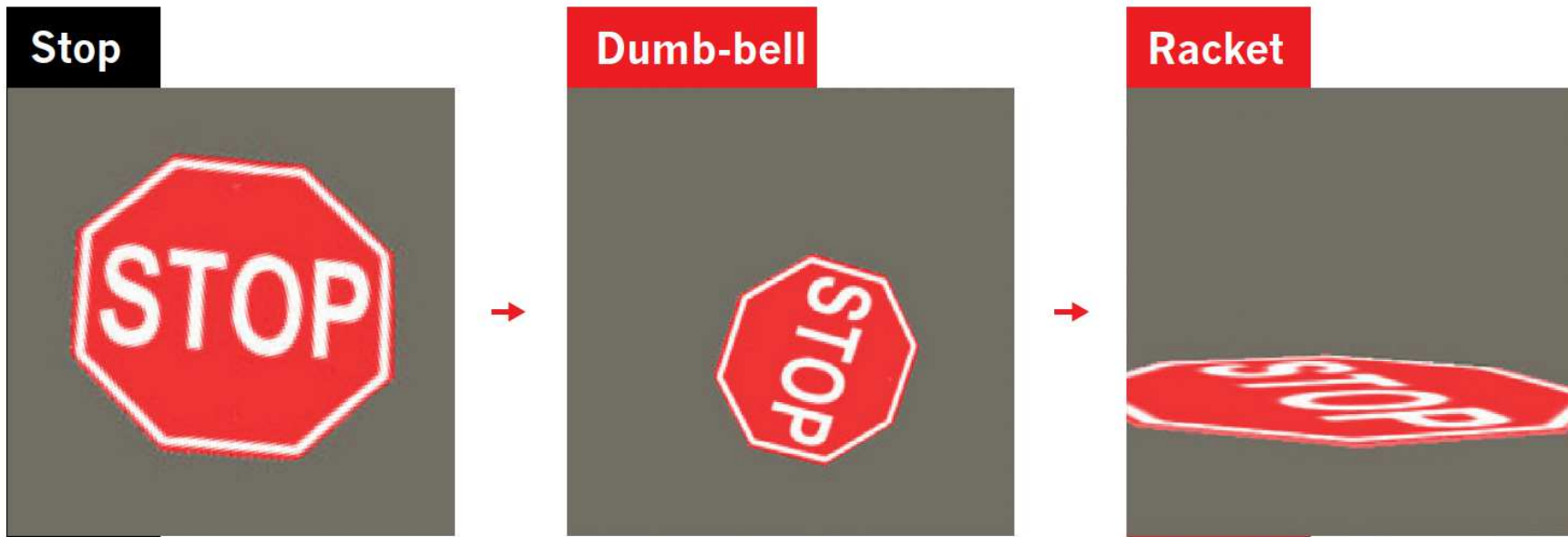
King penguin



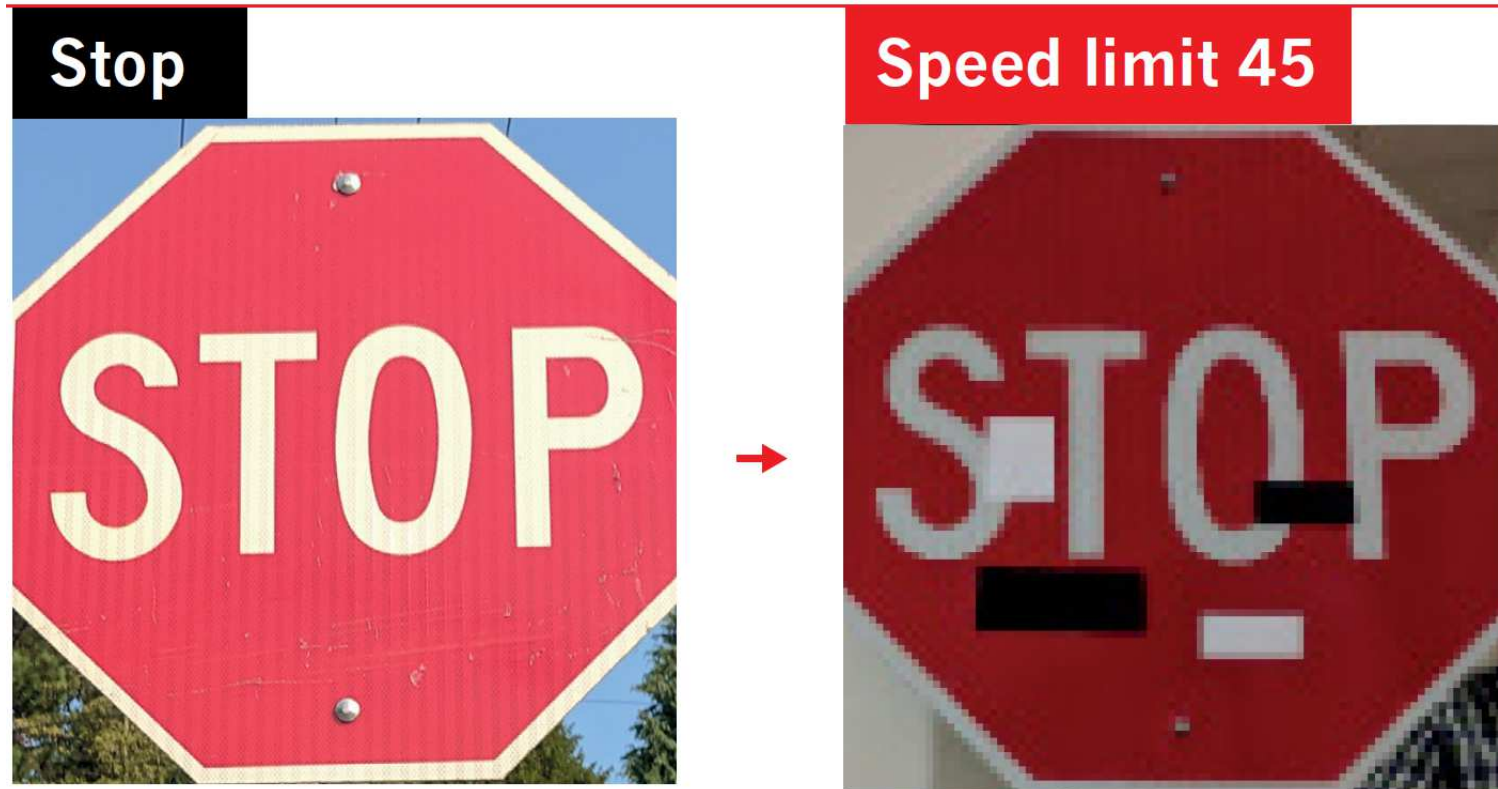
Starfish



# Falsche Perspektive

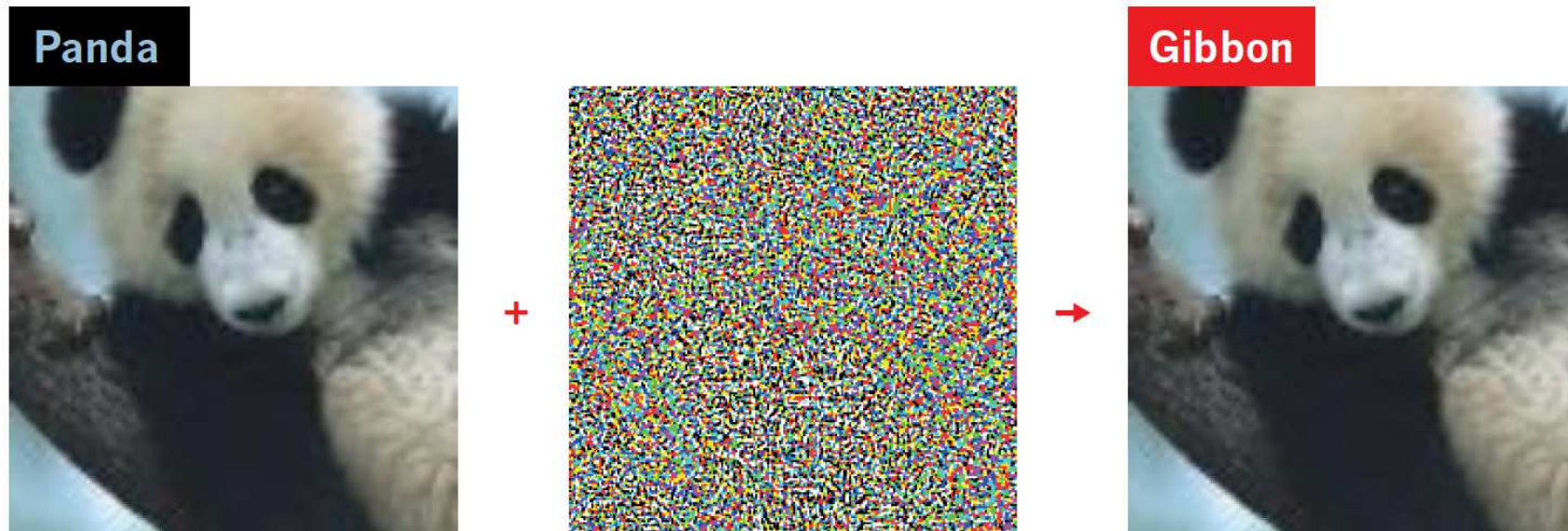


## Gemeine Pflaster



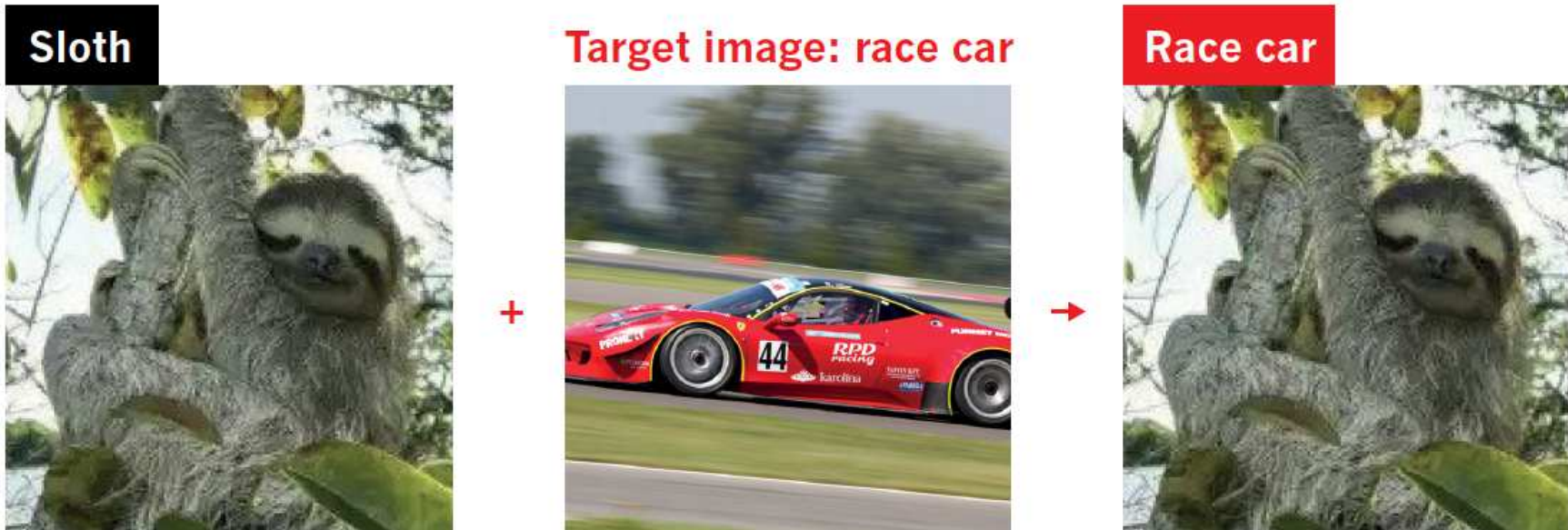


## Gemeines Rauschen



Schlecht konditioniertes Problem? Instabiler Algorithmus?

# Zielsicheres Rauschen Rauschen



Schlecht konditioniertes Problem? Instabiler Algorithmus?